

# Discrete Event Simulation of Physics Lessons in High School Classrooms: an Application in Refraction and Reflection of Light

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## Abstract

This paper describes the application of a model of discrete-event simulation (DES) to be used as a teaching resource in class. Some basic concepts of physics related to refraction and reflection of light, typically taught in high school classes, were simulated. A comparison was made between certain relevant aspects of the simulation models developed for this paper and those of other models having a similar purpose. As a result, we concluded that the models built, in addition to not requiring extensive laboratory resources, offered, as significant advantages, dynamic visualization of the concepts to be taught, the possibility of adapting them to new parameters, and a relative short time for their construction.

**Keywords:** Discrete event simulation, Simulation education, Teaching resource, Physics lessons, Refraction and reflection of light.

# 1 Introduction

In recent works, such as Nascimento and Rangel (2012), Silva and Rangel (2011), Rangel et al. (2011), and Zee and Slomp (2009), an alternative use for discrete-event simulation (DES) as a didactic resource for student learning and training has been demonstrated. Thus, the possibility was raised of extending the boundaries of DES beyond traditional applications of analysis of dynamic and stochastic systems. The fact emerged from the currently-existing facility in constructing simulation models quickly, with a high degree of detail and at a low cost, using a DES package. That is, one may think of constructing small simulation models as a tool in order to enrich teaching a lesson through dynamic examples. Thus, a teacher with limited programming-language skills can create a simulator using the development environments of DES models to demonstrate concepts to be applied in examples of physics situations for classroom environments.

In this way, this paper describes the use of a DES model to be used as a didactic resource. The models were able to demonstrate basic concepts of physics related to refraction and reflection of light, typically taught in high school classes. In this sense, it is expected that a student can visualize the concepts addressed by the simulations as well as better understand the subject being taught in a physics class. A comparison of some relevant aspects was performed, relating the simulation models developed for this paper to other existing ones of similar purpose.

## 1.1 Description of the Physical Phenomenon

This section describes a simulation model to demonstrate the basic concepts of the phenomenon of refraction and reflection of light. It is noteworthy that this simulation model is built only

with the purpose of being able to visualize the animation of the system and, therefore, represent the physical phenomenon of interest. It is worth emphasizing that the purpose here is quite different from typical situations, where a DES model is built to be used as an object of analysis and evaluation of variables related to the dynamic behavior of a given system.

One of the principles of geometrical optics, the law of reflection, states that the reflection angle ( $\theta_1'$ ) of a light ray incident on a smooth surface is equal to the angle of incidence ( $\theta_1$ ). When the incidence occurs on another transparent or semi-transparent physical medium, part of the ray is transmitted ( $\theta_2$ ) as can be seen in Figure 1. This transmitted ray passes through the other medium with a propagation velocity different from the speed of light in a vacuum, and it characterizes a trajectory different from the one that would be traversed in the previous medium.

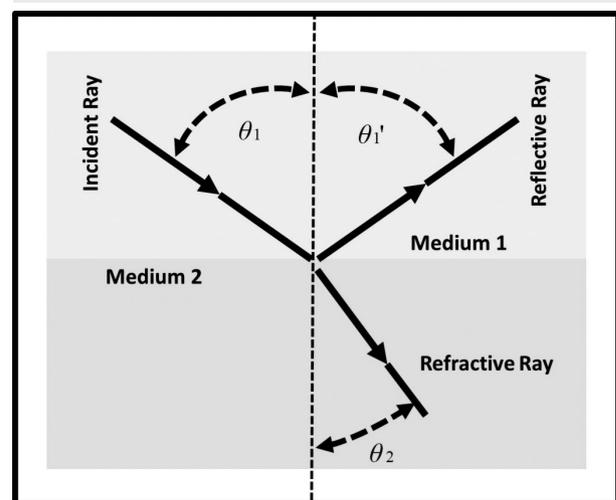


Figure 1: Illustration of the refraction and reflection phenomenon

The law of refraction or Snell's law, shown in Equation 1, expresses the difference of trajectory in terms of the projection angle of the light rays,  $\theta_1$  and  $\theta_2$ , and its relation to the index of refraction of each medium,  $n_1$  and  $n_2$ , respectively.

$$N_1 \sin \theta_1 = N_2 \sin \theta_2 \quad (1)$$

The refractive index of a medium is defined as a relation between the propagation speed in the vacuum and the propagation speed in that medium, as shown in Equation 2.

$$N_{\text{means}} = \frac{V_{\text{vacuum}}}{V_{\text{means}}} \quad \text{where} \quad V_{\text{vacuum}} = 3 \cdot 10^8 \text{ m/s} \quad (2)$$

In a special case, a light ray that propagates in a medium and enters another one with a lower refractive index may not even be refracted. At a certain angle of incidence defined by Equation 2, the whole incident ray is reflected, in an example of what is described as total reflection. Thus, as shown in Figure 2, there will be a value for the angle of incidence, called the critical angle, and  $\sin \theta_2 > 1.0$  in Equation 1.

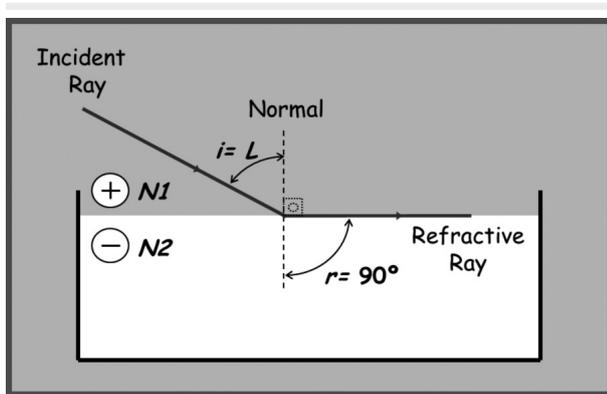


Figure 2: Limit for total reflection – critical angle

## 1.2 Simulation Model

Although light is a continuous phenomenon, the simulation models that illustrated the physical concepts of reflection and refraction of light propagation could be represented in a DES environment, where the entity represented was the light ray.

The methodology used by Banks (2010) was followed to prepare this simulation model according to the following steps: formulation and analysis of the hypothetical problem; construction of the conceptual model; construction of the simulation model; verification and validation; and experimentation.

From the IDEF-SIM technique (Montevechi *et al.*, 2010), it was possible to construct the conceptual model of the process with an easily understandable visual representation and logic similar to that used in programming the computational model. The conceptual model was translated into Arena software in order to carry out the computer simulation.

Thus, two simulation models were constructed to illustrate the light ray changing dynamically across the mediums. In the first, the light propagated from air to water, and, in the second, the ray went from water to air. As the two models were similar, only the model in which the light propagated from air to water was presented.

## 1.3 Air-Water Model

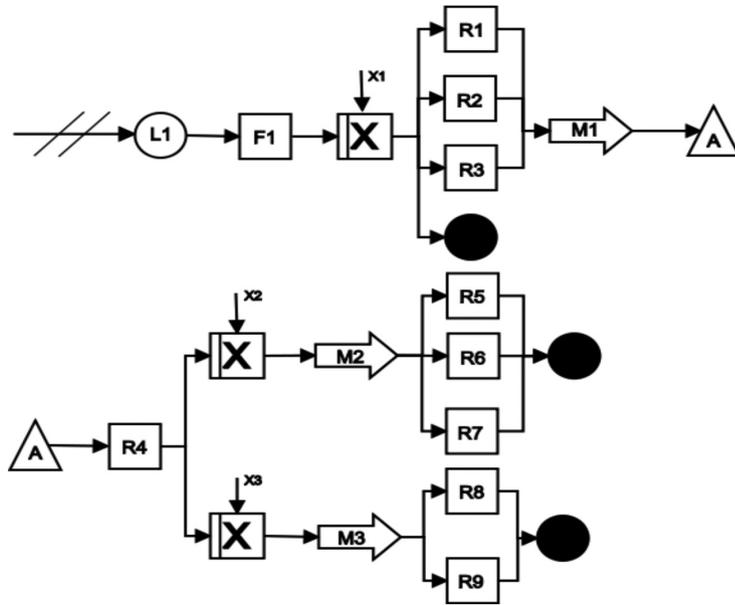
To represent this model, we considered the most commonly used angles of incidence: 30°, 45° e 60°. Figure 3 shows that the light ray was the generated entity and would follow a particular trajectory depending on the attribute, in this case, the angle of incidence chosen by the student through a spreadsheet interface. This trajectory was chosen through three “or” functions, that drove the rays according to their angles.

## 1.4 Experiments

The purpose of the experiments performed was to evaluate whether the constructed models can represent the concepts of the physical phenomena of interest in a clear and easy way.

## 1.5 Air-Water Simulation

Figure 4 shows three instants during the simulation of physical phenomena. In this model, the



Item	Description	Parameters
L1	Light ray entity	Constant, 1 hour; 2 at a time
F1	Queue light ray	Quantity: 1
X1	Or function	If angle = 30° goes to R1 If angle = 45° goes to R2 If angle = 60° goes to R3 If angle = 30°, 45° and 60° goes to S1
R1 to R3	Incident rays	Quantity: 3
M1	Movement to R4	Quantity: 1
R4	Mediums - change in the trajectory of the ray / change of medium (air → water)	Quantity: 1
X2	Or function	If angle = 30° goes to R5 If angle = 45° goes to R6 If angle = 60° goes to R7 If angle = 30°, 45° and 60° goes to S2
X3	Or function	If angle = 30° goes to R8 If angle = 45° goes to R9 If angle = 60° goes to R10 If angle = 30°, 45° and 60° goes to S3
M2	Movement from R5 to R7	Quantity: 1
R5 to R7	Reflected rays	Quantity: 3
M3	Movement from R8 to R10	Quantity: 1
R8 / R9	Refracted rays	Quantity: 3
S1 to S3	Outputs	Quantity: 3

Figure 3: Conceptual model of the reflection and refraction phenomena (AIR-WATER Trajectory).

trajectory followed when the selected attribute of the light entity was 60° could be visualized. In addition to designing the trajectory of the light ray, the animation showed the angles of reflection and refraction according to the angle of incidence chosen. Thus, if the chosen angle of incidence were 60°, the angle of reflection would be equal to 60° and the angle of refraction 41.77°.

### 1.6 Water-Air Simulation

Figure 5, similarly to the one above, also shows three instants of the simulation of the physical phenomena. However, in this case, the trajectory followed when the chosen attribute for the entity was 30° (angle smaller than the limit angle) could be visualized. In addition to designing the trajec-

tory and indicating the predefined limit angle, the animation showed the angle of reflection and refraction according to the angle of incidence chosen. If the chosen angle were 30°, the angle of reflection would be of 30° and that of refraction 41°.

If the angle of incidence chosen were greater than the limit angle, the total reflection of light would occur, since the light would only be reflected and no longer refracted. Figure 6 shows the simulation model that represents that phenomenon. In the example illustrated by the model, the limit angle is 50.28°.

### 1.7 Comparison with other Simulators

Table 1 presents a concise comparison of the simulation models described in this paper with

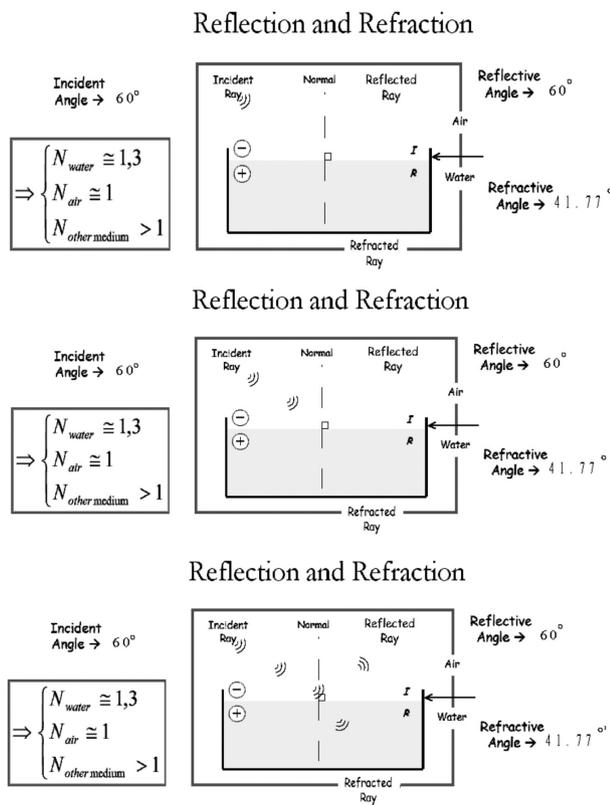


Figure 4: Different moments of the simulation model execution (Trajectory Air-Water).

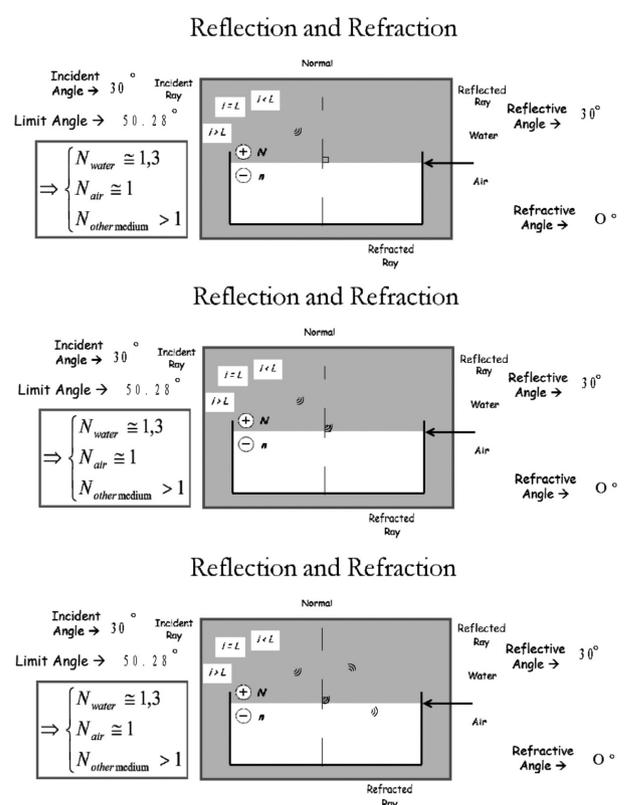


Figure 5: Different moments of the execution of the simulation model (Water-Air Trajectory)

other models developed using general-purpose programming languages. These are as follows: Refraction of Light Simulation (Refraction of Light Simulation, 2012), Reflection / Refraction (Reflection / Refraction, 2012), Refraction Simulator (Refraction Simulator, 2012) and Reflection and Refraction (Reflection and Refraction, 2012).

Analyzing Table 1, it can be seen that other simulators that were found are built using the Java programming language. It is clear that this is a language with many programming resources; however, it requires expert programmers for the development of applications. In contrast, the proposed simulator could be created by a teacher of the discipline in about five hours of development time and learned to use with only twenty hours of training in any development environment of the DES, in this case, Arena.

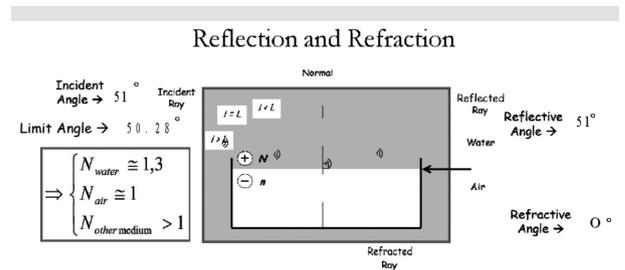


Figure 6: Instant when the angle of incidence was greater than the limit angle (WATER-AIR Trajectory). Total light reflection.

Furthermore, the simulator in DES made it possible for the student to visualize the propagation of the light ray, through movements displayed by the model in real time. The other simulators that were found are more static; despite allowing the changing of characteristics such as angles and the refractive index, as the model in DES also does, they cannot reproduce this animation.

**Table 1: Comparison among simulators in general and the simulator described in this paper.**

Characteristics	Other Simulators	Simulator proposed in DES
Development Environment	Java	ARENA
License	No	No (Academic version)
Interactivity	Yes	Yes
Allows change	No	Yes
Dynamic model	No	Yes
Visualization adjustment	No	Yes

## 2 Concluding Remarks

The experimental simulation models developed for this paper suggest that the proposal presented can be applied in the classroom. Dynamically, the simulators that were developed could show the physics concepts being taught, without the need for extensive laboratory resources.

Concerning the comparison made with the existing simulators, the construction of the didactic models without the need for extensive laboratory resources, using instead a DES package, demonstrated the main advantages to be real-time animation, the possibility of adaptation to new parameters, and the simplicity of the interface.

It is noteworthy that the model described in this paper was developed by a teacher of the discipline who is not a programming expert. Thus, once the teacher is the modeler, he or she can change the model, adapting it to facilitate the demonstration of the concepts being taught.

As future studies, one proposal would be to compare the time required for the construction of the models developed in a DES simulation environment with the time for those built in Java. Furthermore, the extent of specialization

required for the developers of both approaches can be evaluated.

After developing the models, we noticed that there were numerous possibilities for the use of simulated environments to build models that can be used for training of high school and technical students, facilitating learning in the class.

It can also be suggested, for a coming study, to evaluate students' learning using the simulation environment for the representation of the concepts addressed in class and compare it with the performance of students without its help.

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